

TABLE B6

Critical values of the *BCIPS* test with $m=3$ –with an intercept and a linear trend

<i>p</i>	$T \setminus N$	$K=1$					$K=2$					$K=3$					$K=4$					$K=5$					
		20	30	50	100	200	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200	

Notes: Same as those in Table B3 except that \mathbf{h}_t in regression is set to $\mathbf{h}_t = [1, t]$.

TABLE B9

Sizes and Powers of the *BCIPS* test with two known factors ($m=2$) in which factors and idiosyncratic errors are serially uncorrelated –with an Intercept and a linear trend

$T \setminus N$	$K=1$					$K=2$					$K=3$				
	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200
Size															
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, \alpha_{iy,2} \sim \text{i.i.d.}U[1, 2]$, $\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U[1, 2]$															
50	0.052	0.052	0.047	0.040	0.051	0.047	0.046	0.057	0.042	0.058	0.048	0.042	0.047	0.047	0.046
70	0.050	0.049	0.043	0.042	0.045	0.050	0.043	0.052	0.042	0.049	0.049	0.053	0.047	0.049	0.049
100	0.045	0.049	0.044	0.056	0.051	0.048	0.052	0.052	0.042	0.049	0.037	0.051	0.046	0.050	0.053
200	0.041	0.048	0.049	0.050	0.052	0.045	0.045	0.044	0.047	0.046	0.045	0.056	0.044	0.043	0.057
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, -\alpha_{iy,2} \sim \text{i.i.d.}U[10, 20]$, $-\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U[3, 5]$															
50	0.042	0.046	0.056	0.046	0.046	0.051	0.043	0.037	0.053	0.059	0.044	0.040	0.050	0.049	0.050
70	0.042	0.060	0.046	0.046	0.038	0.045	0.052	0.047	0.055	0.050	0.045	0.047	0.048	0.052	0.047
100	0.036	0.037	0.041	0.048	0.052	0.042	0.047	0.047	0.049	0.046	0.056	0.044	0.038	0.054	0.054
200	0.049	0.053	0.049	0.050	0.048	0.050	0.041	0.041	0.043	0.039	0.035	0.060	0.043	0.049	0.049
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, \alpha_{iy,2} \sim \text{i.i.d.}U[10, 100]$, $\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U[3, 5]$															
50	0.048	0.052	0.043	0.044	0.045	0.053	0.043	0.041	0.057	0.068	0.055	0.033	0.043	0.053	0.047
70	0.043	0.038	0.050	0.051	0.044	0.040	0.048	0.044	0.047	0.055	0.058	0.049	0.051	0.046	0.051
100	0.045	0.040	0.045	0.045	0.050	0.049	0.052	0.057	0.043	0.045	0.047	0.045	0.045	0.049	0.056
200	0.048	0.040	0.051	0.049	0.047	0.048	0.043	0.046	0.045	0.037	0.055	0.050	0.042	0.048	0.046
Power:															
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, \alpha_{iy,2} \sim \text{i.i.d.}U(1, 2)$, $\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(1, 2)$															
50	0.154	0.141	0.162	0.148	0.172	0.306	0.302	0.363	0.304	0.412	0.363	0.319	0.390	0.400	0.443
70	0.212	0.309	0.315	0.446	0.459	0.416	0.566	0.575	0.706	0.712	0.513	0.683	0.716	0.840	0.834
100	0.491	0.739	0.714	0.961	0.991	0.765	0.919	0.923	0.992	0.997	0.870	0.978	0.972	1.000	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, -\alpha_{iy,2} \sim \text{i.i.d.}U(10, 20)$, $-\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(3, 5)$															
50	0.102	0.143	0.161	0.156	0.210	0.270	0.326	0.373	0.435	0.528	0.282	0.361	0.398	0.498	0.532
70	0.195	0.309	0.314	0.436	0.569	0.400	0.626	0.611	0.802	0.873	0.516	0.711	0.735	0.883	0.955
100	0.673	0.530	0.819	0.919	0.982	0.922	0.829	0.978	0.990	1.000	0.966	0.923	0.996	1.000	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
<i>BCIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, \alpha_{iy,2} \sim \text{i.i.d.}U(10, 100)$, $\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(3, 5)$															
50	0.107	0.157	0.090	0.097	0.076	0.221	0.266	0.232	0.236	0.269	0.244	0.323	0.270	0.345	0.321
70	0.161	0.199	0.255	0.367	0.341	0.328	0.502	0.510	0.673	0.769	0.498	0.657	0.708	0.855	0.933
100	0.544	0.638	0.875	0.928	0.984	0.890	0.936	0.998	1.000	1.000	0.954	0.986	1.000	1.000	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

Notes: y_{it} is generated as $y_{it} = \mu_{iy}(1 - \phi_t L)t + (1 - \phi_t L)(\mu_i + \alpha_{iy,1} \sin(2\pi\kappa t / T) + \alpha_{iy,2} \cos(2\pi\kappa t / T)) + \phi_t y_{it-1} + \gamma_{iy,1} f_{1t} + \gamma_{iy,2} f_{2t} + \eta_{iyt}$,
 $\eta_{iyt} = \rho_{iy} \eta_{iyt-1} + (1 - \rho_{iy}^2)^{1/2} \varepsilon_{iyt}$, with $y_{i0}, \varepsilon_{iy0} \sim \text{i.i.d.}N(0, 1)$, $\mu_i \sim \text{i.i.d.}N[1, 1]$, $\gamma_{iy,1} \sim \text{i.i.d.}U[0, 2]$, $\gamma_{iy,2} \sim \text{i.i.d.}U[0, 1]$,
 $f_{1t}, f_{2t} \sim \text{i.i.d.}N(0, 1)$, $\varepsilon_{iyt} \sim \text{i.i.d.}N(0, \sigma_t^2)$ with $\sigma_t^2 \sim \text{i.i.d.}U[0.5, 1.5]$; $\rho_{iy} \sim \text{i.i.d.}U[0.2, 0.4]$ and $\sim \text{i.i.d.}U[-0.4, -0.2]$ to denote the case
of positive and negative residual serial correlation, respectively. $x_{it} = x_{it-1} + \alpha_{ix,1} \Delta \sin(2\pi\kappa t / T) + \alpha_{ix,2} \Delta \cos(2\pi\kappa t / T) + \gamma_{ix,1} f_{1t} + \eta_{ixt}$,
 $\eta_{ixt} = \rho_{ix} \eta_{ixt-1} + \varepsilon_{ixt}$, $x_{i0} \sim \text{i.i.d.}N(0, 1)$, $\gamma_{ix,1} \sim \text{i.i.d.}U[0, 2]$, $\rho_{ix} \sim \text{i.i.d.}U[0.2, 0.4]$ and $\varepsilon_{ixt} \sim N(0, 1 - \rho_{ix}^2)$. Sizes (under the null $\phi_t = 1$)
and Powers (under the alternative $\phi_t \sim \text{i.i.d.}U[0.85, 0.95]$) of the *BCIPS* statistic are computed at the 5% nominal level based on the *BCADF*
regression equation. The lag order of the model is selected based on the *SBC* of the panel: $SBC = -\frac{TN}{2}(1 + \ln 2\pi) - \frac{T}{2} \sum_{i=1}^N \ln \left(\frac{\sum_{t=1}^T \hat{\varepsilon}_{it}^2}{T} \right)$,
where T is the number of observations and N is the panel size. The *BCIPS* statistics is described by equation (28).

TABLE B10

Sizes of Pesaran et al.'s (2013) *CIPS* test with two known factors in which factors and idiosyncratic errors are serially uncorrelated—with an Intercept and a linear trend

$T \setminus N$	$\kappa = 1$					$\kappa = 2$					$\kappa = 3$				
	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200
Size: Pesaran's <i>CIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, -\alpha_{iy,2} \sim \text{i.i.d.}U(1, 2)$, $-\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(1, 2)$															
50	0.216	0.194	0.252	0.318	0.386	0.196	0.172	0.190	0.292	0.294	0.058	0.055	0.047	0.069	0.066
70	0.141	0.143	0.181	0.197	0.292	0.108	0.131	0.155	0.220	0.235	0.040	0.039	0.053	0.079	0.061
100	0.117	0.114	0.168	0.229	0.198	0.102	0.093	0.154	0.173	0.181	0.051	0.030	0.077	0.057	0.060
200	0.084	0.100	0.113	0.097	0.102	0.052	0.087	0.085	0.065	0.089	0.028	0.046	0.028	0.031	0.037
Size: Pesaran's <i>CIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, -\alpha_{iy,2} \sim \text{i.i.d.}U(3, 5)$, $-\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(3, 5)$															
50	0.520	0.574	0.574	0.722	0.794	0.338	0.305	0.288	0.398	0.427	0.085	0.062	0.047	0.069	0.060
70	0.364	0.435	0.466	0.621	0.699	0.205	0.249	0.273	0.346	0.439	0.051	0.054	0.058	0.067	0.086
100	0.262	0.347	0.417	0.521	0.546	0.161	0.267	0.275	0.311	0.374	0.057	0.089	0.074	0.071	0.095
200	0.241	0.256	0.279	0.385	0.400	0.243	0.155	0.227	0.276	0.272	0.123	0.049	0.110	0.114	0.094
Size: Pesaran's <i>CIPS</i> (\hat{p}, κ), $\alpha_{iy,1}, -\alpha_{iy,2} \sim \text{i.i.d.}U(10, 20)$, $-\alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(3, 5)$															
50	0.445	0.375	0.877	0.836	0.950	0.214	0.229	0.348	0.376	0.466	0.043	0.045	0.046	0.053	0.079
70	0.380	0.474	0.801	0.651	0.745	0.189	0.270	0.363	0.298	0.360	0.048	0.063	0.070	0.043	0.045
100	0.166	0.391	0.393	0.557	0.686	0.114	0.254	0.190	0.283	0.391	0.032	0.069	0.035	0.053	0.071
200	0.152	0.489	0.367	0.453	0.600	0.066	0.413	0.241	0.363	0.454	0.021	0.173	0.067	0.136	0.156

Notes: Same as those in Table B9.

TABLE B11

Sizes and powers of the *BCIPS* test with two known factors ($m=2$) in which factors are serially uncorrelated but idiosyncratic errors are serially correlated –with an Intercept and a linear trend

$T \setminus N$	$K=1$					$K=2$					$K=3$				
	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200
$\alpha_{iy,1}, \alpha_{iy,2}, \alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.}U(1,2)$															
Size: <i>BCIPS</i> (\hat{p}, κ), positive correlation in idiosyncratic errors															
50	0.058	0.053	0.044	0.043	0.037	0.040	0.033	0.034	0.034	0.041	0.041	0.031	0.024	0.021	0.018
70	0.052	0.054	0.045	0.046	0.033	0.041	0.046	0.039	0.027	0.034	0.031	0.036	0.035	0.019	0.026
100	0.044	0.035	0.041	0.037	0.042	0.049	0.043	0.041	0.031	0.050	0.045	0.027	0.033	0.027	0.041
200	0.050	0.044	0.050	0.048	0.043	0.049	0.050	0.046	0.036	0.048	0.041	0.044	0.038	0.042	0.037
Size: <i>BCIPS</i> (\hat{p}, κ); negative correlation in idiosyncratic errors															
50	0.059	0.057	0.051	0.058	0.057	0.049	0.056	0.059	0.062	0.075	0.066	0.075	0.066	0.080	0.076
70	0.045	0.058	0.052	0.056	0.047	0.054	0.060	0.051	0.051	0.058	0.056	0.064	0.066	0.057	0.074
100	0.040	0.037	0.044	0.048	0.049	0.053	0.050	0.051	0.041	0.065	0.061	0.050	0.063	0.053	0.076
200	0.040	0.040	0.039	0.046	0.042	0.047	0.052	0.052	0.043	0.050	0.047	0.047	0.044	0.051	0.049
Power: <i>BCIPS</i> (\hat{p}, κ); positive correlation in idiosyncratic errors															
50	0.086	0.102	0.085	0.082	0.074	0.160	0.179	0.192	0.204	0.215	0.146	0.167	0.157	0.176	0.184
70	0.112	0.192	0.181	0.193	0.234	0.234	0.373	0.365	0.406	0.454	0.219	0.396	0.413	0.410	0.522
100	0.340	0.322	0.478	0.631	0.733	0.645	0.610	0.791	0.850	0.903	0.725	0.706	0.852	0.946	0.976
200	0.999	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
Power: <i>BCIPS</i> (\hat{p}, κ); negative correlation in idiosyncratic errors															
50	0.100	0.113	0.098	0.093	0.083	0.200	0.224	0.234	0.231	0.257	0.259	0.314	0.297	0.344	0.355
70	0.110	0.226	0.213	0.226	0.283	0.239	0.447	0.433	0.455	0.559	0.311	0.593	0.616	0.644	0.776
100	0.417	0.410	0.623	0.757	0.871	0.704	0.715	0.886	0.928	0.975	0.826	0.852	0.966	0.992	0.999
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

Notes: Same as those in Table B9

TABLE B12

Sizes and powers of the *BCIPS* test with two known factors ($m=2$) in which factors are serially uncorrelated but idiosyncratic errors are serially correlated –with an Intercept and a linear trend

$T \setminus N$	$\mathcal{K}=1$					$\mathcal{K}=2$					$\mathcal{K}=3$				
	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200
$\alpha_{iy1}, -\alpha_{iy2} \sim \text{i.i.d.}U(10, 20), -\alpha_{ix1}, \alpha_{ix2} \sim \text{i.i.d.}U(3,5)$															
Size: <i>BCIPS</i> (\hat{p}, κ), positive correlation in idiosyncratic errors															
50	0.033	0.045	0.049	0.032	0.038	0.036	0.033	0.028	0.029	0.031	0.034	0.024	0.023	0.024	0.020
70	0.046	0.057	0.034	0.049	0.034	0.042	0.042	0.037	0.041	0.031	0.035	0.037	0.032	0.025	0.022
100	0.049	0.044	0.044	0.040	0.049	0.046	0.046	0.042	0.036	0.036	0.049	0.033	0.034	0.034	0.038
200	0.053	0.050	0.052	0.047	0.048	0.051	0.043	0.041	0.042	0.032	0.039	0.062	0.044	0.040	0.038
Size: <i>BCIPS</i> (\hat{p}, κ), negative correlation in idiosyncratic errors															
50	0.039	0.050	0.052	0.054	0.057	0.056	0.054	0.048	0.063	0.073	0.070	0.060	0.073	0.075	0.083
70	0.047	0.060	0.044	0.059	0.039	0.054	0.059	0.051	0.060	0.058	0.059	0.059	0.069	0.065	0.069
100	0.044	0.048	0.040	0.042	0.051	0.050	0.053	0.051	0.050	0.051	0.061	0.046	0.051	0.066	0.069
200	0.045	0.049	0.046	0.044	0.050	0.051	0.041	0.038	0.048	0.042	0.044	0.063	0.043	0.055	0.048
Power: <i>BCIPS</i> (\hat{p}, κ), positive correlation in idiosyncratic errors															
50	0.071	0.090	0.101	0.088	0.107	0.191	0.219	0.240	0.256	0.302	0.150	0.183	0.178	0.206	0.221
70	0.135	0.174	0.157	0.234	0.262	0.292	0.418	0.411	0.581	0.618	0.301	0.426	0.421	0.534	0.616
100	0.381	0.319	0.543	0.609	0.767	0.744	0.676	0.867	0.880	0.954	0.811	0.729	0.924	0.965	0.990
200	0.999	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
Power: <i>BCIPS</i> (\hat{p}, κ), negative correlation in idiosyncratic errors															
50	0.068	0.083	0.083	0.072	0.082	0.185	0.202	0.234	0.239	0.290	0.211	0.278	0.295	0.339	0.368
70	0.127	0.185	0.168	0.220	0.252	0.267	0.441	0.429	0.587	0.649	0.379	0.583	0.599	0.742	0.851
100	0.529	0.383	0.635	0.727	0.887	0.836	0.722	0.917	0.959	0.995	0.929	0.860	0.980	0.998	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
$\alpha_{iy1}, \alpha_{iy2} \sim \text{i.i.d.}U(10,100), \alpha_{ix1}, \alpha_{ix2} \sim \text{i.i.d.}U(3,5)$															
50	0.044	0.045	0.035	0.039	0.032	0.039	0.048	0.031	0.036	0.027	0.040	0.031	0.029	0.024	0.017
70	0.043	0.042	0.040	0.038	0.041	0.033	0.041	0.036	0.036	0.046	0.027	0.034	0.035	0.029	0.024
100	0.045	0.041	0.052	0.051	0.036	0.039	0.054	0.044	0.032	0.036	0.033	0.029	0.037	0.028	0.036
200	0.045	0.043	0.045	0.051	0.042	0.043	0.052	0.043	0.044	0.050	0.051	0.030	0.040	0.042	0.037
Size: <i>BCIPS</i> (\hat{p}, κ), negative correlation in idiosyncratic errors															
50	0.056	0.064	0.050	0.058	0.057	0.059	0.076	0.056	0.076	0.061	0.079	0.079	0.074	0.074	0.080
70	0.053	0.048	0.042	0.054	0.059	0.049	0.052	0.052	0.053	0.072	0.053	0.063	0.068	0.062	0.067
100	0.047	0.044	0.050	0.057	0.046	0.047	0.060	0.056	0.047	0.049	0.059	0.046	0.063	0.054	0.066
200	0.046	0.039	0.044	0.051	0.044	0.053	0.051	0.044	0.054	0.053	0.054	0.038	0.052	0.051	0.040
Power: <i>BCIPS</i> (\hat{p}, κ), positive correlation in idiosyncratic errors															
50	0.168	0.175	0.198	0.224	0.206	0.239	0.231	0.277	0.272	0.298	0.304	0.343	0.390	0.536	0.627
70	0.379	0.355	0.398	0.589	0.733	0.448	0.611	0.743	0.762	0.928	0.588	0.812	0.947	0.970	1.000
100	0.680	0.878	0.987	0.998	1.000	0.920	0.989	1.000	1.000	1.000	0.983	0.998	1.000	1.000	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
Power: <i>BCIPS</i> (\hat{p}, κ), negative correlation in idiosyncratic errors															
50	0.099	0.079	0.090	0.064	0.041	0.342	0.280	0.340	0.413	0.499	0.636	0.650	0.778	0.940	0.992
70	0.350	0.352	0.454	0.537	0.772	0.699	0.901	0.982	0.988	1.000	0.909	0.993	1.000	1.000	1.000
100	0.856	0.959	1.000	1.000	1.000	0.997	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
200	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

Notes: Same as those in Table B9

TABLE B13

Sizes of the BCIPS test with two known factors in which factors are serially uncorrelated and κ is unknown—with an Intercept and a linear trend

$T \setminus N$	$\kappa=1$					$\kappa=2$					$\kappa=3$				
	20	30	50	100	200	20	30	50	100	200	20	30	50	100	200
Size: $BCIPS(\hat{p}, \kappa)$, iid in idiosyncratic errors															
50	0.101	0.087	0.084	0.074	0.083	0.109	0.088	0.082	0.088	0.092	0.113	0.072	0.077	0.086	0.087
70	0.086	0.090	0.074	0.077	0.087	0.092	0.076	0.065	0.086	0.078	0.095	0.073	0.067	0.070	0.070
100	0.075	0.079	0.076	0.068	0.073	0.064	0.068	0.070	0.069	0.064	0.061	0.057	0.060	0.055	0.057
200	0.080	0.080	0.075	0.071	0.072	0.072	0.072	0.063	0.068	0.057	0.050	0.054	0.043	0.039	0.040
Size: $BCIPS(\hat{p}, \kappa)$, positive correlation in idiosyncratic errors															
50	0.097	0.082	0.077	0.067	0.072	0.120	0.104	0.100	0.109	0.100	0.120	0.086	0.084	0.090	0.089
70	0.096	0.085	0.076	0.082	0.074	0.117	0.091	0.079	0.096	0.095	0.102	0.079	0.058	0.073	0.063
100	0.092	0.083	0.085	0.076	0.074	0.086	0.087	0.085	0.085	0.084	0.064	0.064	0.058	0.060	0.042
200	0.090	0.088	0.085	0.076	0.079	0.084	0.084	0.081	0.082	0.073	0.061	0.063	0.046	0.038	0.026
Size: $BCIPS(\hat{p}, \kappa)$, negative correlation in idiosyncratic errors															
50	0.100	0.091	0.084	0.076	0.081	0.104	0.092	0.086	0.105	0.098	0.117	0.095	0.104	0.113	0.125
70	0.086	0.086	0.070	0.078	0.084	0.090	0.073	0.070	0.087	0.079	0.095	0.086	0.072	0.087	0.091
100	0.075	0.075	0.076	0.062	0.070	0.063	0.067	0.074	0.066	0.070	0.066	0.061	0.069	0.066	0.076
200	0.078	0.075	0.069	0.064	0.071	0.065	0.061	0.059	0.060	0.054	0.050	0.062	0.050	0.054	0.056

Notes: Same as those in Table 1. $\alpha_{iy,1}, \alpha_{iy,2}, \alpha_{ix,1}, \alpha_{ix,2} \sim \text{i.i.d.} U(1,2)$. Numbers in the table are the sizes of the $BCIPS$ statistic in which the frequency parameter (κ) in the Fourier function and the lag order of the model are jointly selected based on the method discussed in section 3.6. The $BCIPS$ statistics is described by equation (28).

TABLE B14

The *BCIPS* and *CIPS* panel unit-root tests for real exchange rates

$$\Delta q_{it} = c_{i,0} + c_{i,1} \sin(2\pi kt / T) + c_{i,2} \cos(2\pi kt / T) + \mathbf{c}'_{i,3} \bar{\mathbf{z}}_{t-1} + \mathbf{c}'_{i,4} \Delta \bar{\mathbf{z}}_t + \sum_{j=1}^p \mathbf{c}'_{i,5,j} \Delta \bar{\mathbf{z}}_{t-j} \\ + \sum_{j=1}^p c_{i,6,j} \Delta q_{i,t-j} + b_i q_{i,t-1} + e_{it}, \quad \text{where } \mathbf{z}_{it} = (q_{it}, \mathbf{x}'_{it})'.$$

Included \mathbf{x}_{it}	$(\hat{p}, \hat{\kappa})$	$[N, T]$	<i>CD</i>	<i>BCIPS</i>	<i>CIPS</i>
$\hat{p} = \text{Int} \left[4 \{ \min(N, T) / 100 \}^{0.25} \right]$					
m=1					
No	(2,1)	[29,124]	115.9	-3.396**	-2.074
m=2					
\overline{gdp}	(2,1)	[19,124]	83.2	-3.700**	-2.822**
$\overline{p_{oil}}$	(2,1)	[29,124]	115.9	-3.181*	-2.131
$\overline{\bar{r}^L}$	(2,1)	[20,124]	97.7	-3.257*	-2.624**
\overline{pd}	(2,1)	[16,124]	73.9	-3.198	-2.658**
m=3					
$\overline{gdp}, \overline{p_{oil}}$	(2,1)	[19,124]	83.2	-3.310	-2.995**
$\overline{p_{oil}}, \overline{\bar{r}^L}$	(2,1)	[20,124]	97.7	-2.966	-2.714*
$\overline{\bar{r}^L}, \overline{gdp}$	(2,2)	[17,124]	79.6	-3.507**	-2.863**
$\overline{pd}, \overline{gdp}$	(2,3)	[15,124]	68.0	-3.967**	-3.426**
$\overline{pd}, \overline{p_{oil}}$	(2,1)	[16,124]	73.9	-2.982	-2.739*
$\overline{pd}, \overline{\bar{r}^L}$	(2,1)	[15,124]	68.1	-3.087	-2.648*
m=4					
$\overline{gdp}, \overline{p_{oil}}, \overline{\bar{r}^L}$	(2,1)	[17,124]	81.4	-3.316	-2.873**
$\overline{pd}, \overline{p_{oil}}, \overline{\bar{r}^L}$	(2,1)	[15,124]	68.1	-2.825	-2.604
$\overline{gdp}, \overline{pd}, \overline{\bar{r}^L}$	(2,2)	[15,124]	66.6	-3.960**	-3.386**
$\overline{gdp}, \overline{p_{oil}}, \overline{pd}$	(2,1)	[15,124]	68.1	-3.268	-2.321**

Notes: m is the number of factors in the model. *CD* is the cross-sectional dependence test of Pesaran (2004). The Bold faced numbers indicate significance at the 5% level. ‘**’ indicates significance at the 1% level and ‘*’ indicates significance at the 5% level. $\hat{\kappa}$ and \hat{p} are jointly determined based on the rule of minimum sum of square described in section 3.6.